Monads

# Monads

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### **Notes: Computerphile Monads**

Consider a data constructor for an expression which captures integer division:

```
1 Data Expr = Val Int | Div Expr Expr
```

Let's write a function that can evaluate these expressions:

```
1 eval :: Expr -> Int
2 eval (Val n) = n
3 eval (Div x y) = (eval x) `div` (eval y)
```

But this is unsafe: if you attempt division by 0 you'll get an error. So let's define a safe division operation

```
1 safediv :: Int -> Int -> Maybe Int
2 safediv n m = if m == 0
3 then Nothing
4 else Just (n `div` m)
```

Now we can rewrite eval to be safe:

Now we have a program that will work safely. But it's pretty ugly and verbose. How can we make it better, and look more like the original code, while still being safe?

First observe that there's a common pattern here: 2 case analyses, doing the same thing. Let's abstract this out, introducing m, f:

1 case m of
2 Nothing -> Nothing
3 Just x -> f x

And let's give a name to this  $m \ge f$ :

```
1 m >== f = case m of
2 Nothing = Nothing
```

```
Just m -> f m
```

With this definition, let's rewrite eval:

This is equivalent to the last definition of eval, but we've abstracted away all the case analyses. But we can still do better, with the syntactic sugar of the **do** notation, which gives a helpful shorthand for programs of this sort:

This is much nicer. All the failure management is handled automatically.

#### Where do the monads come in?

So what does all this have to do with monads? Effectively we have rediscovered the Maybe monad, which comprises 3 things: the Maybe type constructor, and 2 functions:

• **return** :: a -> Maybe: a bridge between the pure and the impure

• >>= :: Maybe a -> (a -> Maybe b)-> Maybe b: sequencing

That's all a monad is:

- 1. Type constructor
- 2. return definition
- 3. >>= definition

#### What's the point?

- 1. The same idea works for other effects: I/O, mutable state, non-determinism, ... Monads give a uniform framework for thinking about programming with effects.
- 2. Supports pure programming with effects: i.e. gives you a way to do impure things in a pure language

- 3. Use of effects is explicit in types: evaluator function here takes an Expr and returns a Maybe Int. You explicitly state what effects may be produced.
- 4. Provides ability to write functions that work for any effect, **effect polymorphism**. Haskell has libraries of generic effect functions.